

## RBF-Elman Neural Network Control on Electro-Hydraulic Load Simulator

Xiaohua Wang<sup>1,a</sup>, ShuaiWu<sup>1,b</sup> and Zongxia Jiao<sup>1</sup>

<sup>1</sup>School of automation science and electrical engineering,  
Beijing University of Aeronautics and Astronautics, Beijing, 100191,China

<sup>a</sup>wxhpc@163.com, <sup>b</sup>wushuai.vip@gmail.com

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**Abstract.** Due to load simulation system existing strong disturbance, parameters time-variation and nonlinear, there was low control precision, poor adaptive ability and robustness in traditional control algorithm. In order to improve load simulation performance, The RBF-Elman neural network-based adaptive control method is presented. In this way, the load simulator system is identified by the RBF-Elman neural network identifier, which provides model information (Jacobian matrix) to the PID controller and synchronous compensator in order to make it adaptive. Back-propagation algorithms are used to train neural network. The PID controller which is designed by requirement for steady can overcome the shortcoming of the neural network controller. Finally, the simulations confirm that this control scheme results in a quick response, robustness, and excellent ability against disturbance.

### Introduction

As a key equipment of hardware-in-loop loading simulation, The main function of the load simulator is reproduced rudder-suffered aerodynamic loads during the aircraft flight in the laboratory, in order to verify the control parameters of the aircraft control system, test load ability of rudder system, shorten aircraft development cycle, save development costs, improve reliability and success rate [1,2]. Load simulator has three forms: hydraulic, electric and pneumatic [3]. Due to hydraulic systems high power/mass ratio, fast response and high stiffness, electro-hydraulic load simulators are widely used. Hydraulic systems are complex and pose nonlinearities, which makes the modeling and design of feedback controllers challenging. The nonlinearities mainly remain in servo valve flow-pressure characteristics, orifice area openings, variations of fluid volume under compression and in part, mechanical friction, damping coefficient, viscosity and elasticity of oil [1,4,5]. In this condition, conventional PID controllers do not yield reasonable performance over a wide range of operating conditions and meet the requirements of control precision, simultaneously ability against disturbance is poor. Therefore, adaptive, self-learning and high-precision is urgent needs of a new load simulator.

When Radial basis function (RBF) neural network simulates nonlinear continuous function, it has fast learning speed, small calculation and no local extrema, which can be applied to real-time control [6]. However, lack of the feedback information, feedforward network structure can't identify dynamic systems effectively, which is difficult to meet the high precision control of dynamic systems. So RBF is integrated with dynamic recurrent neural network, which can improve approximation and identification of dynamic systems and take advantage of RBF rapid calculation and no local extrema. Therefore, the RBF-Elman neural network (RENN) application in real-time and high precision load simulator control system is possible. So, on the one hand, neural network integrated with PID controller (NNPID), based on conventional PID controller, use neural network adaptive ability to fine-tune the system control parameters and constitute self-tuning, stabilizing controller [7,9]. On the other hand, neural network compensator (NNC) is built based on the principles of velocity synchronizing control [1], fine-tuning synchronous control parameters for disturbance-reduced.

### RBF-Elman Neural Network Model

Elman is an important type of recurrent neural networks, because of the addition of the layer or layers feedback connections, therefore it has been widely used in control engineering fields. Based on Elman neural network, three RENN structure [11] is shown in Fig. 1. Compared with feedforward neural

network, besides the input layer, hidden layer and output layer, RENN has a special structural unit called context unit, which is used to receive and memory hidden layer historical information, so it is regarded as a delay operator.

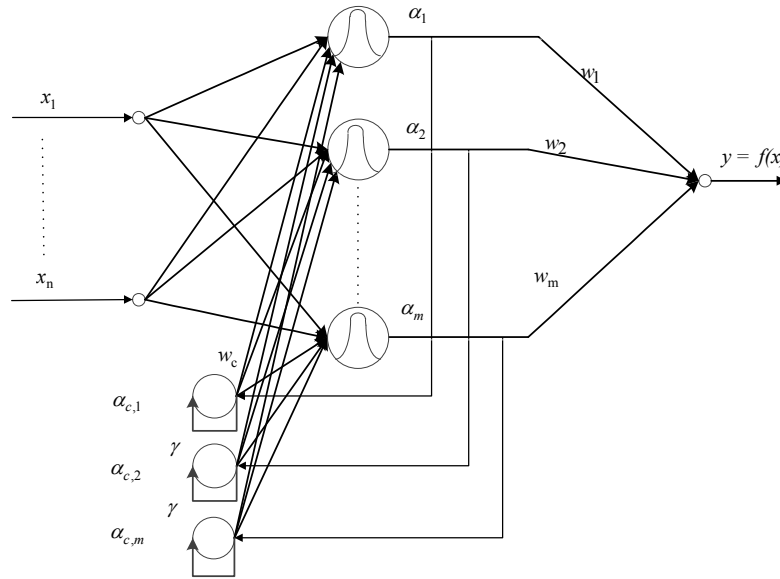


Fig.1 RENN structure diagram

The first layer is the input layer, the layer is connected directly to input value which is transferred to the next layer.

The second layer is hidden layer, whose role is nonlinear mapping using Gaussian function, where, the input-output relationship is:

$$s(j) = \sum_{l=1}^m \omega_{jl}^1 \alpha_{c,l}(k) + \sum_{i=1}^n x_i \tag{1}$$

$$\alpha_{c,l}(k) = \gamma \cdot \alpha_{c,l}(k-1) + \alpha_l(k-1) \tag{2}$$

$$\alpha_j(k) = f[s(j)] = \exp\left[-\left(\frac{s(j) - c_l}{\sigma_l}\right)^2\right] \tag{3}$$

Where:  $i = 1, 2, \dots, n$ ,  $j = l = 1, 2, \dots, m$ ,  $\omega_{jl}^1$  are weights context unit to hidden layer,  $\alpha_j$  are hidden layer output,  $\alpha_{c,j}(k)$  are context unit output,  $c_l$  and  $\sigma_l$  is the center and width of the Gaussian function.  $\gamma$  is context unit feedback gain,  $s$  represents the total input to hidden layer unit,  $k$  means the number of iterations.

The third layer is the output layer, the weighted sum of hidden layer output:

$$y(k) = \sum_{l=1}^m w_l^2 \alpha_l(k) \tag{4}$$

Where:  $y$  is the output of neural network output layer,  $w_l^2$  are weights hidden layer to output layer.

### RENN-based Control Scheme on Electro-Hydraulic Load Simulator

In this section, as shown in Fig. 2, the RENN is derived to model the load simulator system, and then a neural network PID controller and compensator are designed to control it. The control objective is to tune the parameters in the RENN identifier so that its output  $M_m(k)$  can model the system nonlinear behavior  $M(k)$  in real time, at the same time, to tune the parameters in the NNPID controller and NNC so that the output  $M(k)$  of the nonlinear system tracks the desired trajectories  $M_r(k)$ . Therefore, the RENN identifier can provide updated model information (Jacobian matrix) to the NNPID controller and NNC every timestep [13].

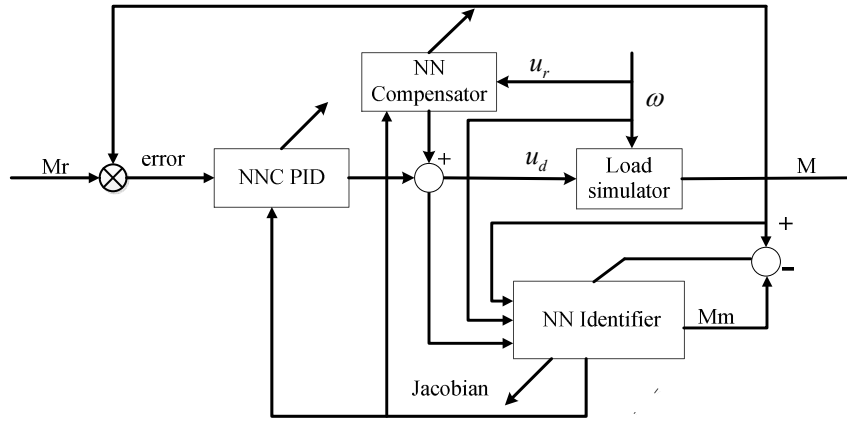


Fig. 2Based on RENNadaptive neural network control system block diagram

**Neural network identifier.** When neural network identifier (NNI) is used to approach power actuator transfer function, model identification accuracy directly determines the neural network control precision. Load Simulator servo valve control signal, torque Sampling and rudder angular velocity are used as NNI inputs.

$$X = [x_1, x_2, x_3]^T = [u, M, \omega]^T \quad (5)$$

In the neural network training strategy, the weights are updated by BP algorithm. The performance target of identification is given as

$$E_m = \frac{1}{2} [M(k) - M_m(k)]^2 = \frac{1}{2} e^2(k) \quad (6)$$

Where:  $M(k)$ ,  $M_m(k)$  and  $e(k)$  are the load simulator output, the RENN output and the identification error, respectively. The optimization target is characterized to minimize the error function Eq. (6) with respect to the adjustable parameter of the network.

By gradient descent method, the neural NNI update rule is calculated as

$$\begin{aligned} w_l^2(k+1) &= w_l^2(k) - \eta_w \left. \frac{\partial E_m}{\partial w_l^2} \right|_k & \omega_{jl}^1(k+1) &= \omega_{jl}^1(k) - \eta_\omega \left. \frac{\partial E_m}{\partial \omega_{jl}^1} \right|_k \\ c_j(k+1) &= c_j(k) - \eta_c \left. \frac{\partial E_m}{\partial c_j} \right|_k & \sigma_j(k+1) &= \sigma_j(k) - \eta_\sigma \left. \frac{\partial E_m}{\partial \sigma_j} \right|_k \end{aligned} \quad (7)$$

Connection weights  $w_l^2$  hidden layer to output layer is calculated as

$$\left. \frac{\partial E_m}{\partial w_l^2} \right|_k = \frac{\partial E_m}{\partial M_m(k)} \cdot \frac{\partial M_m(k)}{\partial w_l^2} = -(M_m(k) - M(k)) \cdot \alpha_l(k) \quad (8)$$

Connection weights  $\omega_{jl}^1$  context unit to hidden layer is calculated as

$$\left. \frac{\partial E_m}{\partial \omega_{jl}^1} \right|_k = \frac{\partial E_m}{\partial M_m(k)} \cdot \frac{\partial M_m(k)}{\partial \alpha_l(k)} \cdot \frac{\partial \alpha_l(k)}{\partial \omega_{jl}^1} = -(M_m(k) - M(k)) \cdot \omega_l^2(k) \cdot \frac{\partial \alpha_l(k)}{\partial \omega_{jl}^1} \quad (9)$$

Where:

$$\frac{\partial \alpha_l(k)}{\partial \omega_{jl}^1} = f'(\bullet) \left[ \alpha_{c,l}(k) + \sum_{j=1}^m \omega_{jl}^1 \frac{\partial \alpha_{c,l}(k)}{\partial \omega_{jl}^1} \right] \quad (10)$$

Not consider  $\alpha_{c,j}(k)$  dependence on weight  $\omega_{jl}^1$ , it is simplified as

$$\begin{aligned} \frac{\partial \alpha_l(k)}{\partial \omega_{jl}^1} &= f'(\bullet) \alpha_{c,l}(k) = f'(\bullet) \alpha_l(k-1) + \gamma \cdot f'(\bullet) \alpha_{c,l}(k-1) \\ &= f'(\bullet) \alpha_l(k-1) + \gamma \cdot \frac{\partial \alpha_l(k-1)}{\partial \omega_{jl}^1} \end{aligned} \quad (11)$$

Center parameter  $c_l$  is calculated as

$$\left. \frac{\partial E_m}{\partial c_l} \right|_k = \frac{\partial E_m}{\partial M_m(k)} \bullet \frac{\partial M_m(k)}{\partial \alpha_l(k)} \bullet \frac{\partial \alpha_l(k)}{\partial c_l} = -(M_m(k) - M(k)) \bullet \omega_l^2(k) \bullet \frac{2\alpha_l(k)[s(l) - \bar{c}_l(k)]}{\sigma_l(k)^2} \quad (12)$$

Similarly, width parameter  $\sigma_l$  is calculated as

$$\left. \frac{\partial E_m}{\partial \sigma_l} \right|_k = \frac{\partial E_m}{\partial M_m(k)} \bullet \frac{\partial M_m(k)}{\partial \alpha_l(k)} \bullet \frac{\partial \alpha_l(k)}{\partial \sigma_l} = -(M_m(k) - M(k)) \bullet \omega_l^2(k) \bullet \frac{2\alpha_l(k)[s(l) - c_l(k)]^2}{\sigma_l(k)^3} \quad (13)$$

From above derivation, for the adjustment of weights  $\omega_{jl}^1$  structural unit to hidden layer, Eq. (11) constitutes a dynamic recursive relation of gradient  $\frac{\partial \alpha_l(k)}{\partial \omega_{jl}^1}$ , so RENN can identify high order systems.

$\frac{\partial M}{\partial u}$  is Jacobian information of the controlled object.  $\frac{\partial M_m}{\partial u}$  is obtained through RENN online identification on load simulation. When NNI approach the controlled object accurately,  $\frac{\partial M_m}{\partial u}$  can replace  $\frac{\partial M}{\partial u}$  as Jacobian matrix.

$$\frac{\partial M}{\partial u} \approx \frac{\partial M_m}{\partial u} = \sum_{i=1}^m \frac{\partial y(k)}{\partial \alpha_i(k)} \bullet \frac{\partial \alpha_i(k)}{\partial z_j} \bullet \frac{\partial z_j}{\partial \Delta u} = \sum_{j=1}^m w_j^2 \bullet f' \bullet \frac{2[c_j(k) - u]}{[\sigma_j(k)]^2} \quad (14)$$

**Neural network controller.** RENN can automatically memory part of the historical information and is more suitable for nonlinear dynamic system identification for the reason of internal dynamic feedback link. Therefore neural network controller can accurately track the electro-hydraulic load simulator model changes, so proposed control scheme can update NNPID control parameters in real time using NNI to ensure the good characteristics of the system.

Conventional PID control principle is given as the following formula

$$error(k) = M_r(k) - M(k) \quad (15)$$

$$xc(1) = error(k) - error(k - 1), \quad xc(2) = error(k) \quad (16)$$

$$xc(3) = error(k) - 2error(k - 1) + error(k - 2) \quad (17)$$

$$u_1(k) = u_1(k - 1) + \Delta u_1(k), \quad \Delta u_1(k) = k_p xc(1) + k_i xc(2) + k_d xc(3) \quad (17)$$

Error function is given as

$$E_l(k) = \frac{1}{2} error(k)^2 \quad (18)$$

Three control parameters can be updated respectively through the gradient descent method

$$\Delta k_p = -\eta \frac{\partial E_l}{\partial k_p} = -\eta \frac{\partial E_l}{\partial M} \bullet \frac{\partial M}{\partial u} \bullet \frac{\partial u}{\partial k_p} = \eta error(k) \frac{\partial M}{\partial u} xc(1) \quad (19)$$

$$\Delta k_i = -\eta \frac{\partial E_l}{\partial k_i} = -\eta \frac{\partial E_l}{\partial M} \bullet \frac{\partial M}{\partial u} \bullet \frac{\partial u}{\partial k_i} = \eta error(k) \frac{\partial M}{\partial u} xc(2) \quad (20)$$

$$\Delta k_d = -\eta \frac{\partial E_l}{\partial k_d} = -\eta \frac{\partial E_l}{\partial M} \bullet \frac{\partial M}{\partial u} \bullet \frac{\partial u}{\partial k_d} = \eta error(k) \frac{\partial M}{\partial u} xc(3) \quad (21)$$

The scheme is based on the traditional PID control theory, which can follow the classical stability theory to determine the range of control parameters to solve the ubiquitous unstable issues in neural network controller. In order to ensure stable operation of the system, the control parameters varies in the following range

$$k_{p \min} \leq k_p \leq k_{p \max}, \quad k_{i \min} \leq k_i \leq k_{i \max}, \quad k_{d \min} \leq k_d \leq k_{d \max}$$

**Neural network compensator.** NNC is based on velocity synchronizing control to compensate disturbance, whose input is rudder servo valve control signal.

Load simulator control signals  $u$  include two parts: NNPID controller value  $u_1$  and NNC  $u_2$ .

$$u = u_1 + u_2 \quad (22)$$

The structure of NNC is single-layer network, the output is  $u_2(k) = u_2(k-1) + \Delta u_2(k)$ ,  $\Delta u_2(k) = k_r(u_2(k) - u_2(k-1))$  (23)

Similarly, NNC parameter is updated as

$$\Delta k_r = -\eta_b \frac{\partial E_1}{\partial k_r} = -\eta_b \frac{\partial E_1}{\partial M} \cdot \frac{\partial M}{\partial u} \cdot \frac{\partial u}{\partial k_r} = \eta_b \text{error}(k) \frac{\partial M}{\partial u} (u_2(k) - u_2(k-1)) \quad (24)$$

Similarly, in order to ensure stability, the compensation parameters vary in the following range

$$0 \leq k_r \leq k_{r,\max}$$

### Simulation Analysis

Load simulator and rudder system model is created using AMESim dynamic simulation integrated environment, neural network control system is created using Matlab-Simulink environment. Through co-simulation between Matlab and AMESim, the ability against disturbance and dynamic tracking characteristics of the proposed method is verified.

**Extraneous Torque Eliminating.** In simulation, rudder motion:  $\theta(t) = 5 \sin(4\pi t)$ . Load simulator instruction is 0.

Fig. 3 shows a comparison of extraneous torque eliminating between conventional PID controller and neural network controller. It is seen from Fig. 3, the extraneous torque produced by proposed RENN-based intelligent control method is too much smaller than that produced by conventional PID control method. NNPID controller can achieve a better elimination effect. The reason is that the neural network controller can adjust parameters in real time according to tracking error changes, reduce extraneous torque, enable the system to track load spectrum accurately.

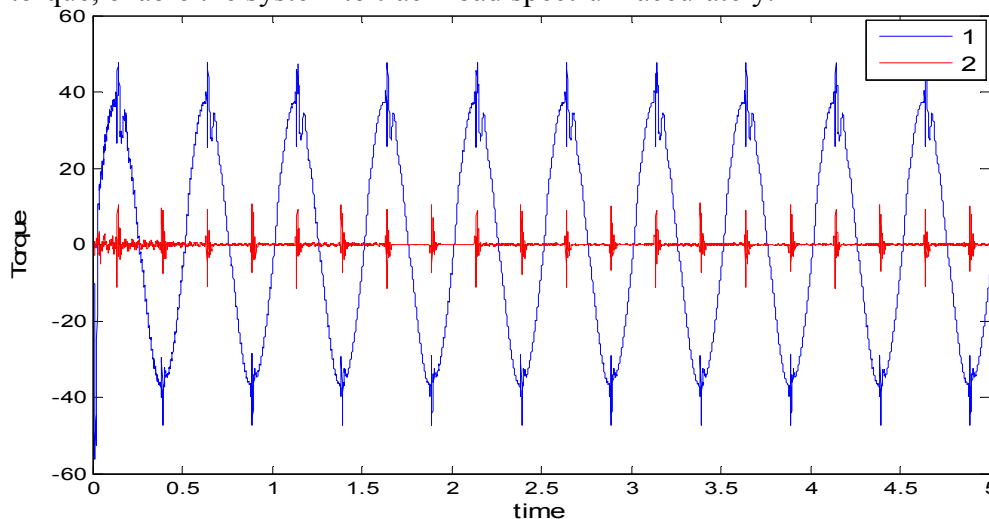


Fig. 3a comparison of extraneous torque eliminating

1. Conventional PID controller method
2. RENN-based intelligent control method

In control process, extraneous torque mutation of load simulation occurred in rudder commutation process.

**Dynamic Load Tracking.** Rudder motion:  $\theta(t) = 5 \sin(4\pi t)$ . Load simulator is tracking tested under different frequency sinewave. It is seen from Fig. 4 and Fig. 5, which show sinusoidal load spectrum tracking. Neural network control scheme not eliminate extraneous torque simply, but use extraneous torque to compensate system tracking lag, which reflect neural network adaptive and self-learning ability. In addition, neural network excellent nonlinear mapping ability results in a quick response, mini phase lags and high control precision.

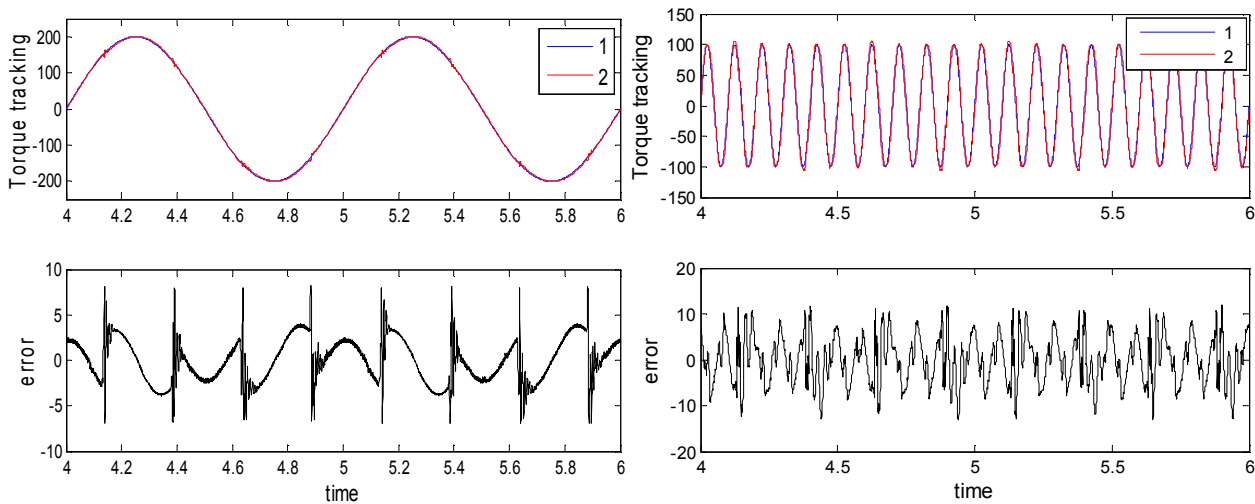


Fig.4 1Hz sin wave tracking error Fig.5 10Hz sin wave tracking error

1. Given load command
2. System load output

Judging from the overall effect, the proposed control method has good tracking speed, robustness and control precision. This is because neural network nonlinear mapping and adaptive ability can solve electro-hydraulic load simulator system nonlinearity, uncertainty and time-variation. Therefore it can get good control effect.

## Conclusions

The RBF-Elman neural network-based intelligent PID controller mainly use RBF-Elman high precision function approximation ability to track the object model change in realtime, on the basis, adjusting control parameters of neural network-based PID controller and compensator, finally, the proposed control scheme can achieve a high control precision. Since neural network PID controller is based on PID control theory, parameters variation ranges are limited to stability theory, which can ensure the stability of system and improve the convergence speed. Furthermore, neural network compensator is based on velocity synchronizing control theory for extraneous force compensation, using neural network adaptivity to achieve a good eliminating effect.

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